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# Routing and Topology Control in Mobile Ad Hoc Networks

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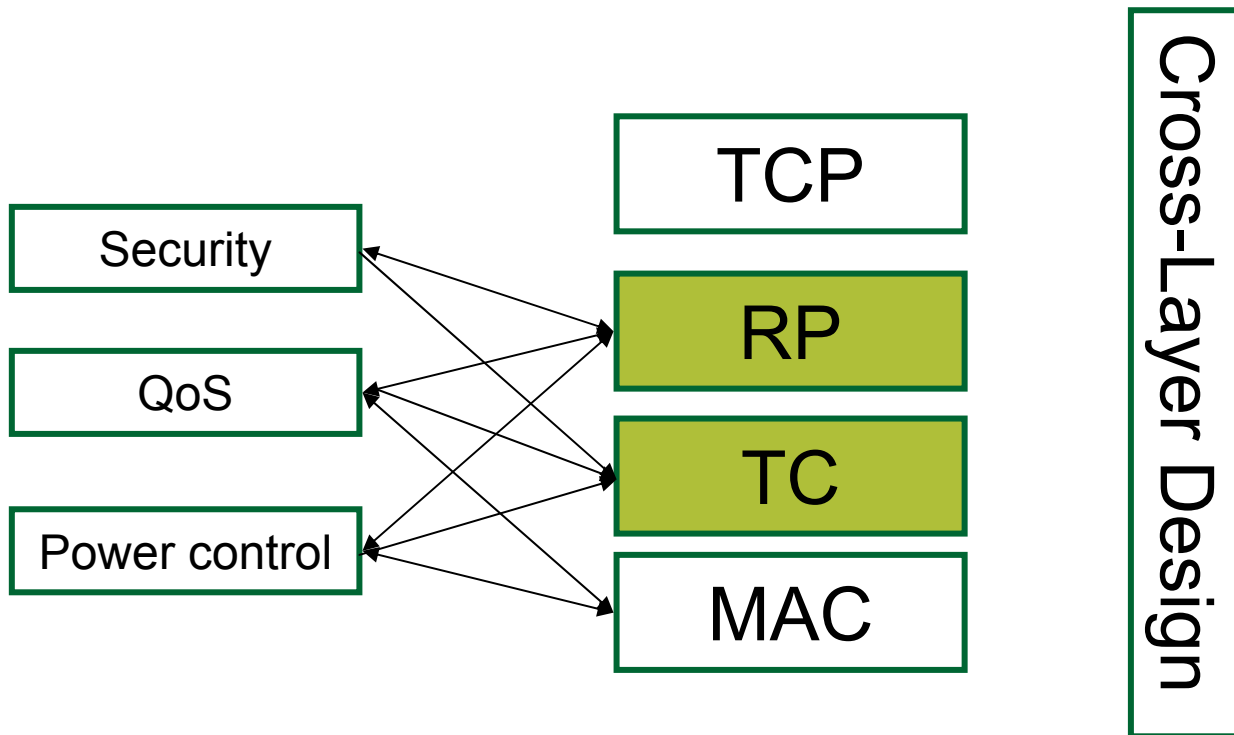
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# Outline



## Capacity of Wireless Ad Hoc Network

# Ad Hoc Networks

- A collection of nodes forming one or several dynamic autonomous networks
  - Nodes may be mobile or fixed
  - Nodes communicate
    - using wireless medium
    - without necessarily the intervention of any fixed infrastructure, i.e. AP/BS
    - potentially in *multi-hop* (store-and-forward) fashion due to the lack of any infrastructure, limited transmission range, channel utilization considerations, power saving
  - Nodes acts as a host, and may act as a router
- Ad Hoc :: Multi-Hop :: Packet Radio Networks

# Routing & Topology Control: Classification

- Ad hoc routing can be broadly classified into topology- and position-based routing strategy
  - Broadcasting, one-to-all
  - Unicasting, one-to-one
  - Multicasting, one-to-some
  - Geocasting, one-to-region
- Topology control
  - Neighborhood discovery
  - Network discovery
  - Backbone formation

# Routing Definition

- A mechanism by which traffic is directed and transported through the network from a source to a destination [steenstrup]
- Core routing functionalities:
  - Route generation
  - Route selection
  - Data forwarding
  - Route maintenance
- Why is routing in ad hoc networks different?

# Topology Control Definition

- Adjust network topology according to some given criteria as environment changes to achieve certain properties
- Such criteria are:
  - K-Connectivity
  - Energy efficiency
  - Scalability
  - Network efficiency
- Why topology control in ad hoc networks?

# Routing and topology control Issues

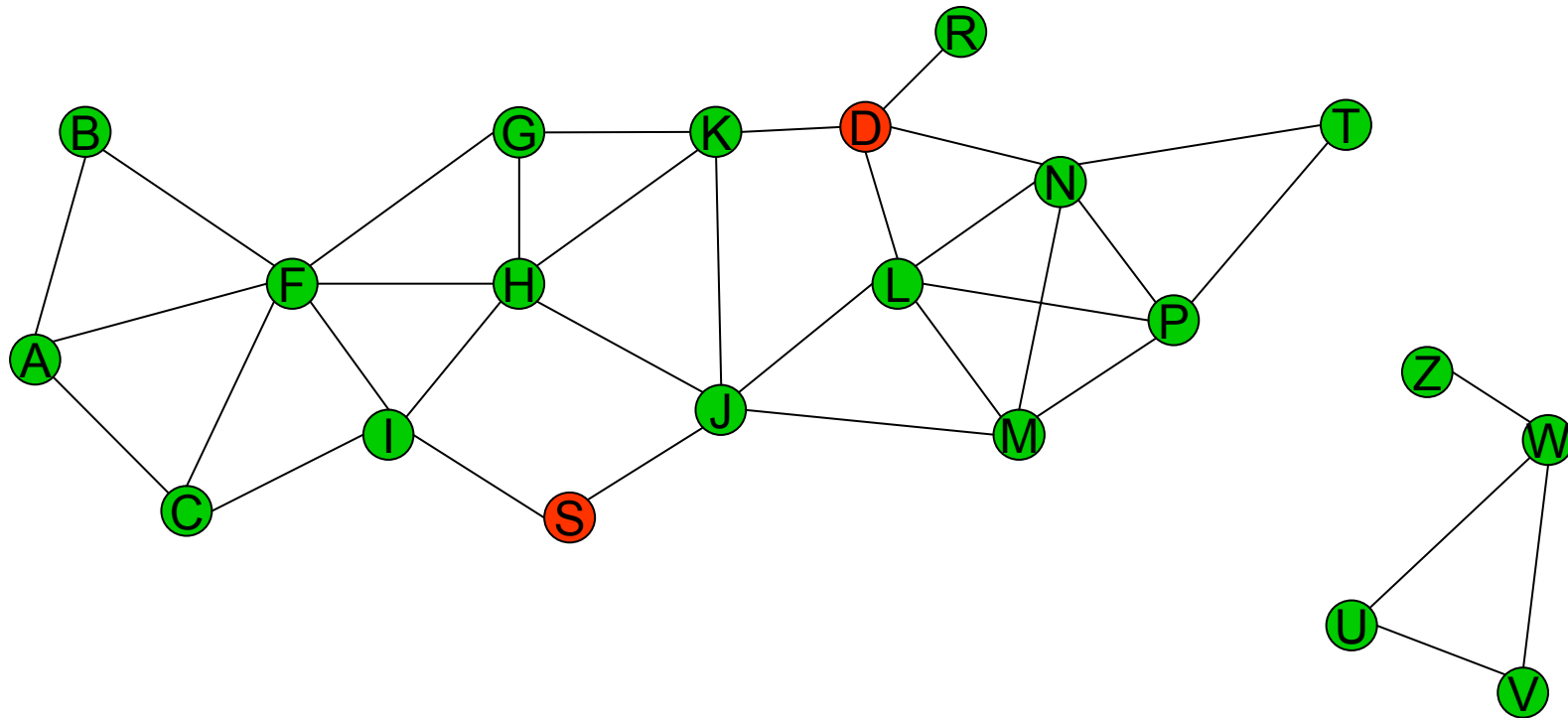
- Routing: topology- / position- based
  - Broadcasting, one-to-all
  - Unicasting, one-to-one
  - Multicasting, one-to-some
  - Geocasting, one-to-region
  
- Topology control
  - Neighborhood discovery
  - Network discovery
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# Broadcasting

- Network wide broadcasting “**flooding**” is one of the building block of ad hoc routing
  - Each node retransmits a copy of the same received **data packets** to its neighbors
  - **Sequence numbers** are used to dump the process of packet generation and duplication
- Why flooding?
- What are the advantages and drawbacks of flooding?



# Flooding



Represents source and destination nodes

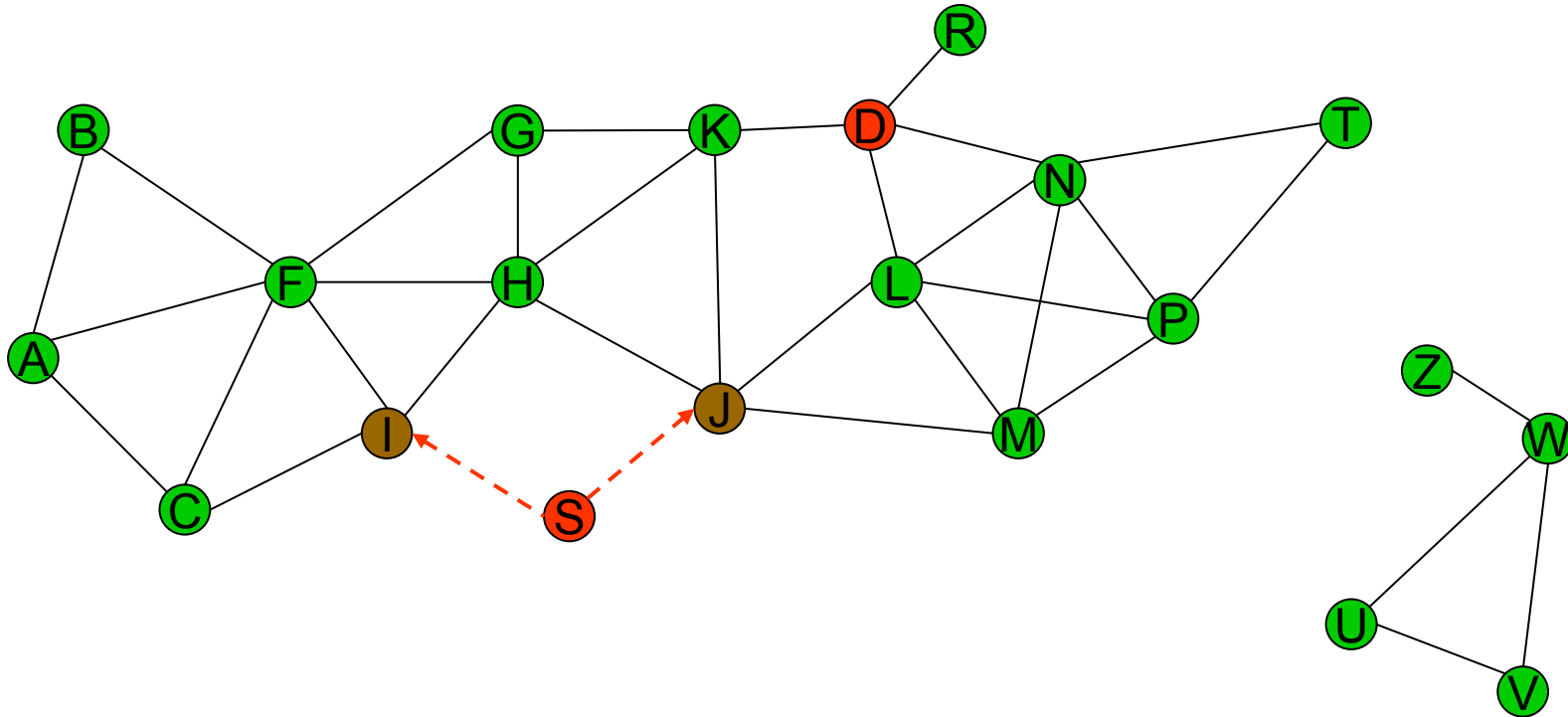


Represents the network nodes



Represents the network connectivity

# Flooding

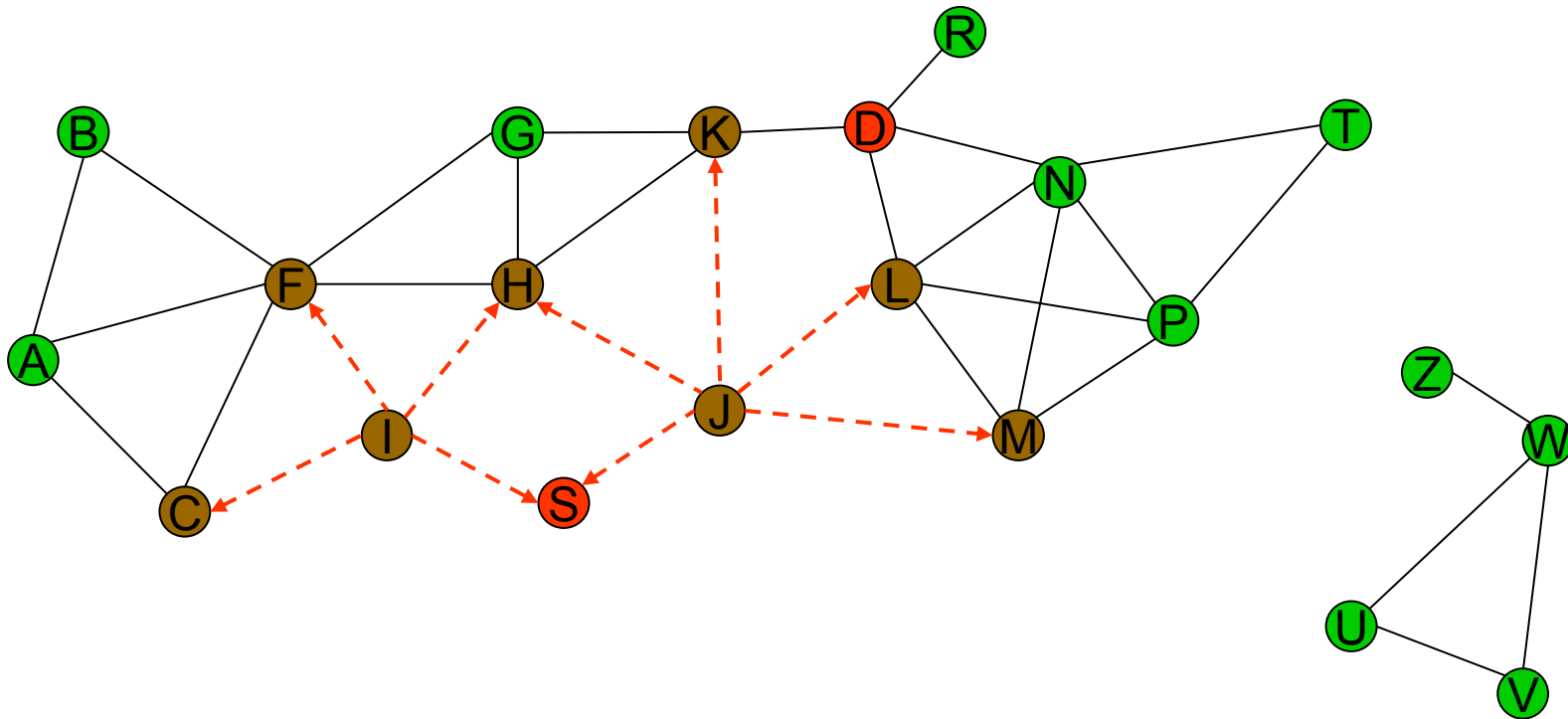


Represents a node that receives packet P for the first time



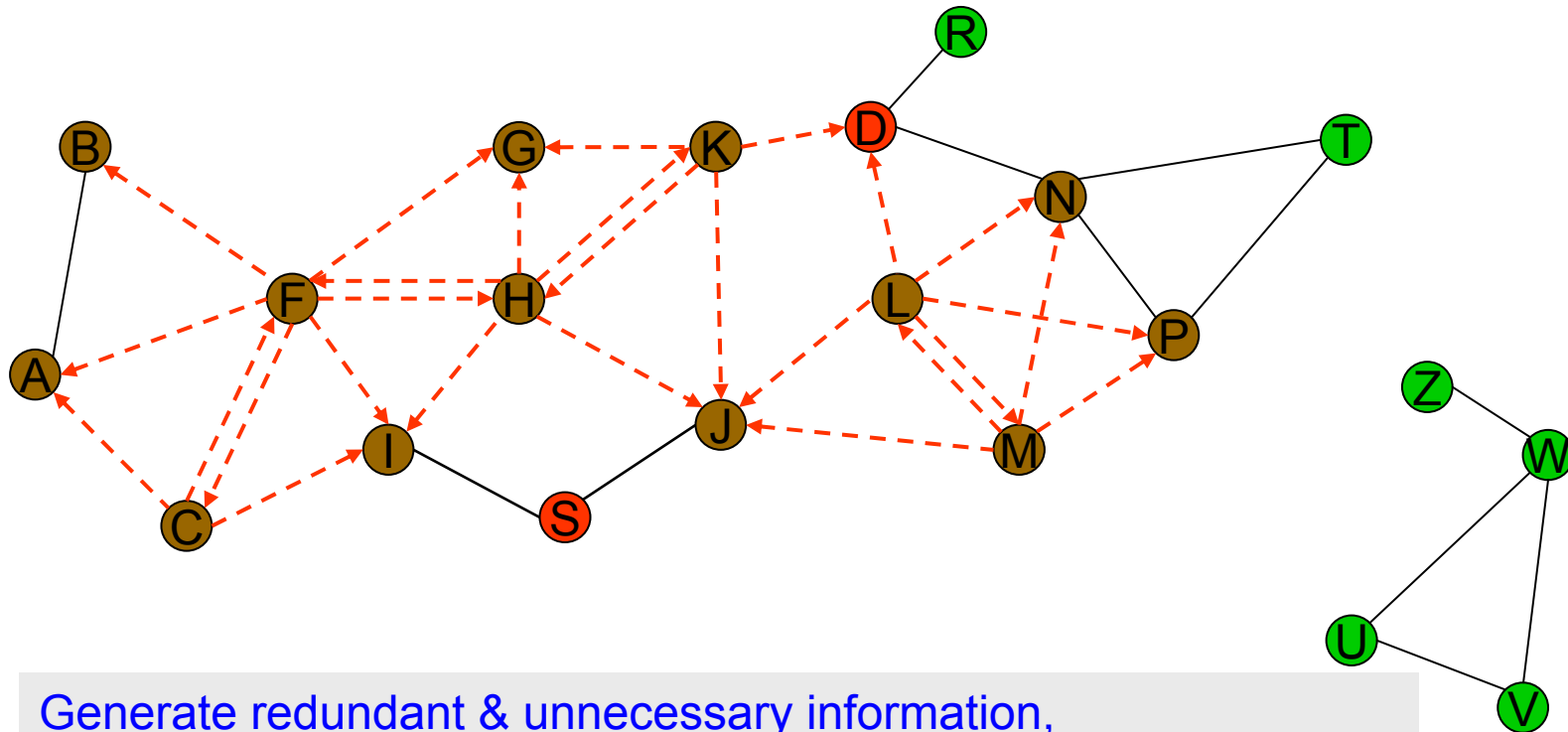
Represents transmission of packet P

# Flooding



Potentially generates collision under random access channel,  
e.g. at node H,  
Note that I & J are hidden from each other

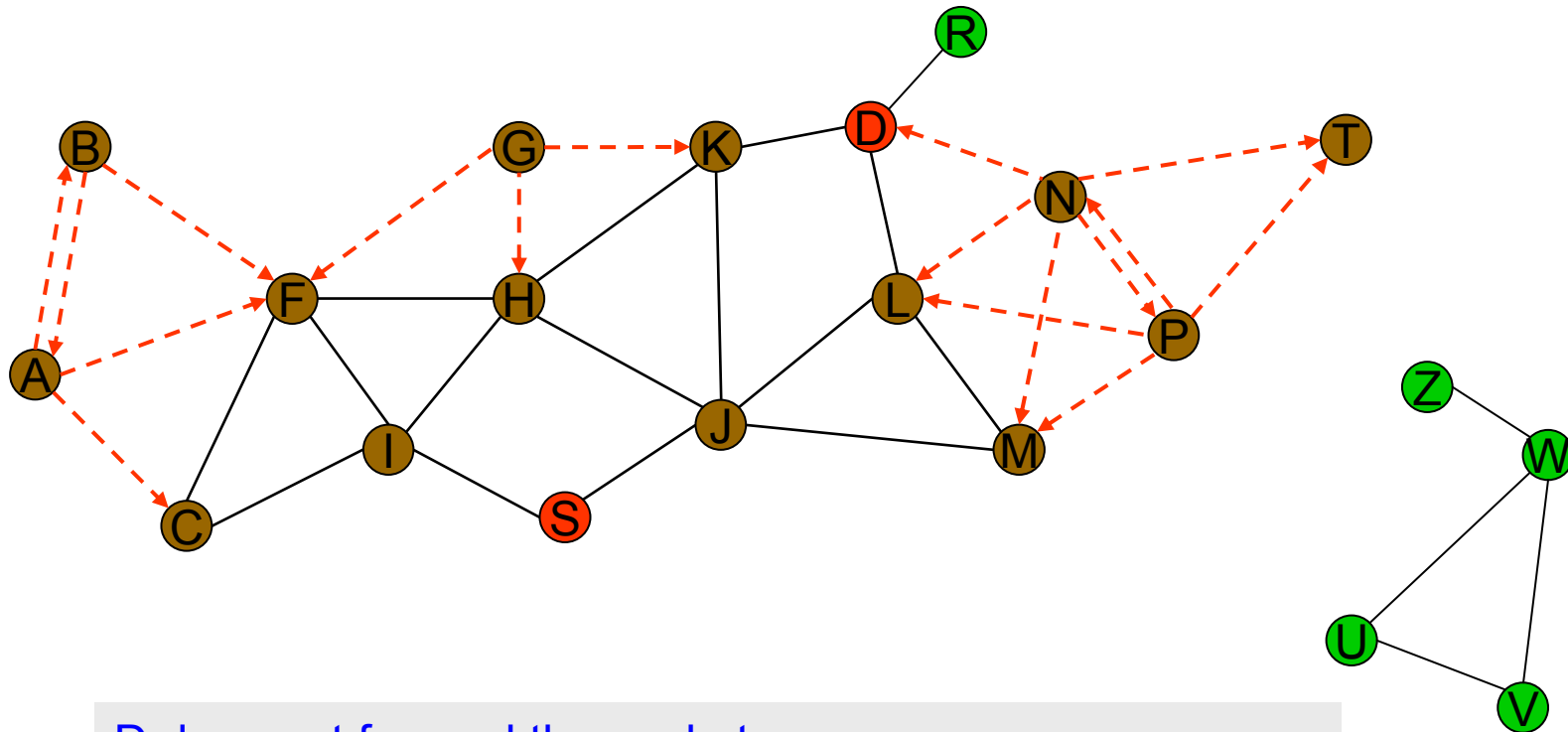
# Flooding



Generate redundant & unnecessary information,  
e.g. node G receives multiple copies of the same message  
Note that node H does not forward the packet P again due to SN

Transmission may collide at D:  
Packet P may not be delivered to the destination

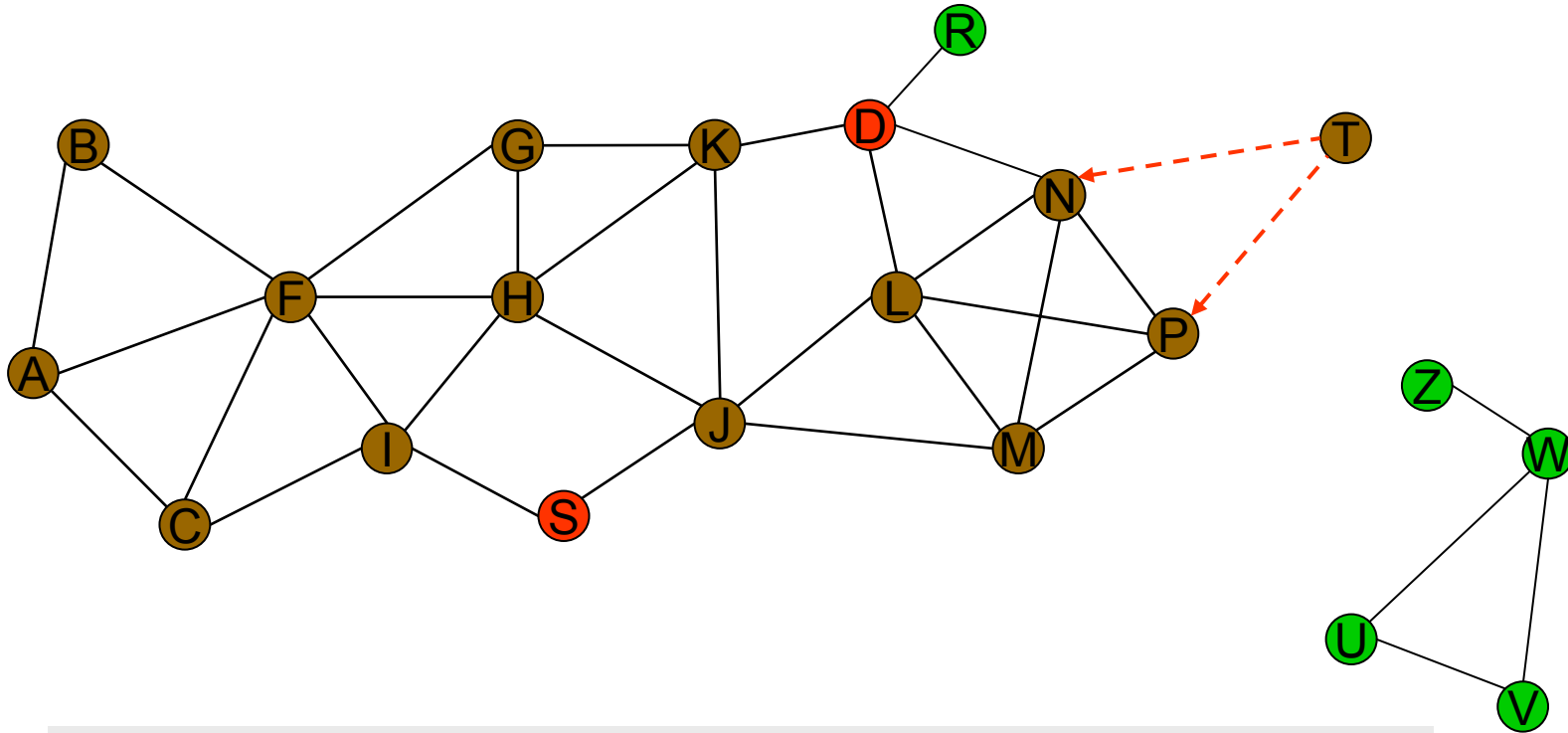
# Flooding



D does not forward the packet  
Flooding is omni-directional (blind)  
e.g. node A & B receive the packet P

Flooding may not converge to the shortest path (hop #)  
e.g.  $P \langle s,d \rangle = (S, J, L, N, D)$

# Flooding



Flooding range is network diameter (TTL)  
e.g. node T receives the packet P

Note: unreachable nodes (e.g. Z) or nodes for which destination is the only upstream node (e.g. R) do not receive the packet P

# Flooding: pros and cons

- Simple
- Multiple path to destination: path diversity
  - Not necessarily the shortest path
- High redundancy, contention, and collision
- High overhead
  - Omni-direction: angle
  - Network diameter: scope

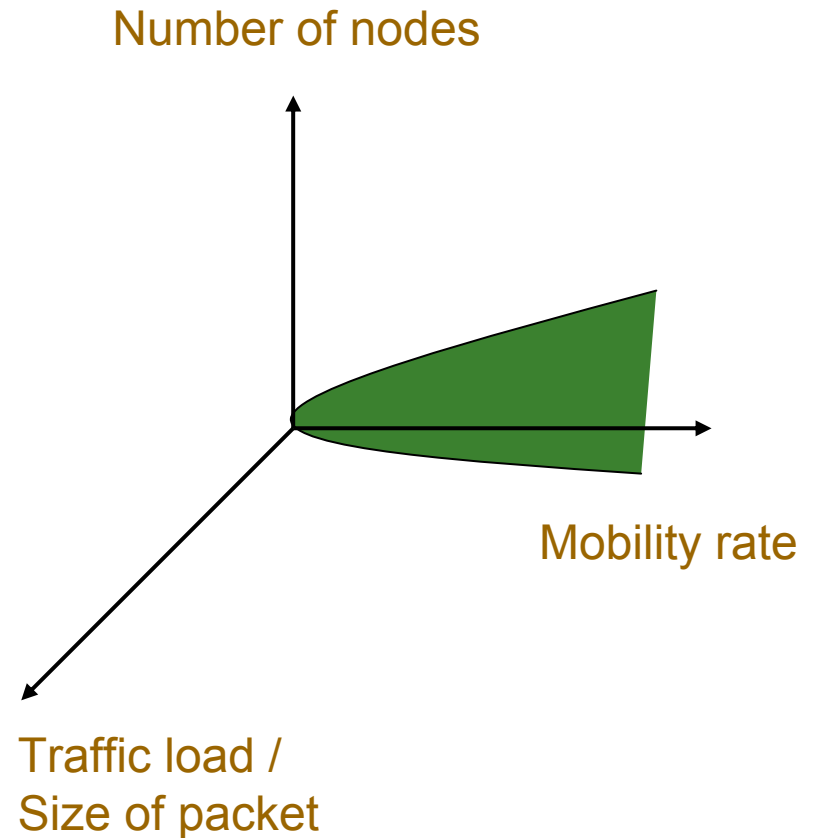
# Protocol scalability [santivanez02]

- The ability of a network to maintain the performance when its limiting factors grow
- Main limiting factors:
  - Mobility rate
  - Traffic load
  - Number of nodes
- Other limiting factors:
  - Packet size
  - Network density



# Flooding scalability

- Is flooding more appropriate for data packet or for control packet?
  - e.g. control packets used for route discovery
  - Depends on the overhead of control packets over data packets transmitted
- How flooding can be improved?



# Flooding

- How to limit the scope of flooding?
  - Query localization technique [[Castenada99](#)]
  - Relative distance estimation RDMAR [[Aggelou99](#)]
  - Expanding ring search [[hassan04](#)]
- How to reduce the angle of flooding?
  - Location aided routing LAR [[ko00](#)]
  - Distance routing effect algorithm for mobility [basagni98]
  - Relative movement estimation RME [nikaein03]
- How to reduce the redundancy ?
  - Broadcast storm problem [ni99]
  - Broadcasting techniques [camp02]
  - Topology control [[rajaraman02](#)]

# Routing and topology control Issues

- Routing: **topology- / position- based**
  - Broadcasting, one-to-all
  - **Unicasting, one-to-one**
  - Multicasting, one-to-some
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# Topology-based Routing: Uniscasting

- Use the information about the sequence of nodes towards destination for forwarding
  - Without location information
- Dilemma at a node:
  - Do I keep track of routes to all destinations, or instead keep track of only those that are of immediate interest?
    - **Proactive**: keep track of all, e.g. LS, DV(DBF), OLSR
    - **Reactive**: only those of immediate interests, DSR/AODV
    - **Hybrid**: partial proactive/partial reactive, e.g. ZRP
- Is there any alternative forwarding strategy?

# Example: Dynamic Source Routing

- Source node initiates a route generation procedure by **flooding** a route request (RREQ)
- Each intermediate nodes append its own ID during the path generation phase
- Upon receiving the **first** RREQ by the destination node, a route reply (RREP) is sent back through the reverse path to the source node
  - RREP piggybacks the route traversed by RREQ
  - Note: The metric used for route selection depends on the traffic load and its distribution
  - Observation: packet size is a function of source-destination distance and nodes' ID size (larger header w.r.t. payload)
  - Question: What happens if the link is unidirectional?

# Example: Dynamic Source Routing

- Source node caches the route included in RREP
  - Optimization: all intermediate nodes or the nodes that overhears the RREQ/RREP can cache the route to react to future RREQs
    - Speedup RREQ, and reduce the overhead
  - But beware:
    - Stale or invalid cached routes can pollute the network and hence affecting the routing performance
    - Reply storm problem
- Source node routes all its data packets by tagging them with the complete route to be traversed
  - Routing is done by the source: **Source Routing**
  - All intermediate nodes determine the next hop based on the tag information

# Example: Ad Hoc On-Demand Distance Vector Routing

- RREQ procedure in AODV is similar to DSR
- Instead of source routing, AODV routes a packet on hop-by-hop basis
  - During RREQ propagation, several reverse routes towards the source node are set up
  - RREP then activates only one of the reverse path by reversing the route toward the destination
  - Note: routing information is stored at each hop
    - Packets do not need to contain routing information
- Neighborhood discovery using hello message
- Reducing flooding overhead using destination sequence number

# Example: Optimized Link-State Routing

- Neighborhood discovery (2-hop)
  - Each node periodically transmits a hello messages
- Multi-Point Relay (MPR) formation
  - Set of nodes over which a broadcasting message propagates
- Link state information (LSI) propagation
  - Each node broadcast the LSI to its neighbors
  - Each neighbor that belongs to the set of MPR re-broadcasts the received LSI
    - Note: In original LS algorithm, all neighbors rebroadcasts the LSI
- Routing table construction
  - Create the network topology and assign a weight for each link
  - Apply shortest path algorithms, such as Dijkstra
  - Determine the next hop for each destination
- Does OLSR adapt its reaction to traffic load / mobility rate ?



# Example: Zone Routing Protocol

- **Intra-zone routing:** Pro-actively maintain state information for links within a short distance from any given node
  - Routes to nodes within short distance are thus maintained proactively (using, link state or distance vector protocol)
- **Inter-zone routing:** Use a route discovery mechanisms for determining routes to far away nodes
  - Route discovery is similar to DSR with the exception that route requests are propagated via peripheral nodes

# Trade-offs

- Delay before data forwarding
  - Proactive protocols may experience lower delay than that of reactive **subject to the frequency of topology changes** since all routes are generated in advance
- Overhead of route generation/maintenance
  - Reactive protocols may produce lower overhead than that of proactive **subject to the frequency of E2E connections** because routes are generated on-demand
- Trade-offs depend on the mobility model and traffic pattern
- Note: all of the aforementioned routing protocols apply flooding in one way or another

# Routing Design Choice

- Whether each node has to perform the same routing functionalities or instead perform some extra functionalities of interest?
  - **Flat structure:** perform same functionalities
  - **Hierarchical structure:** extra functionalities of interest
    - Essentially, in heterogeneous environments where some nodes have some extra capabilities/responsibilities
      - Capability: processing, transmission range, battery life
      - Responsibility: position in the network, speed of movement
    - Can be logical or geographical.
    - What are the examples of hierarchical structure?
    - What are the trade-offs?

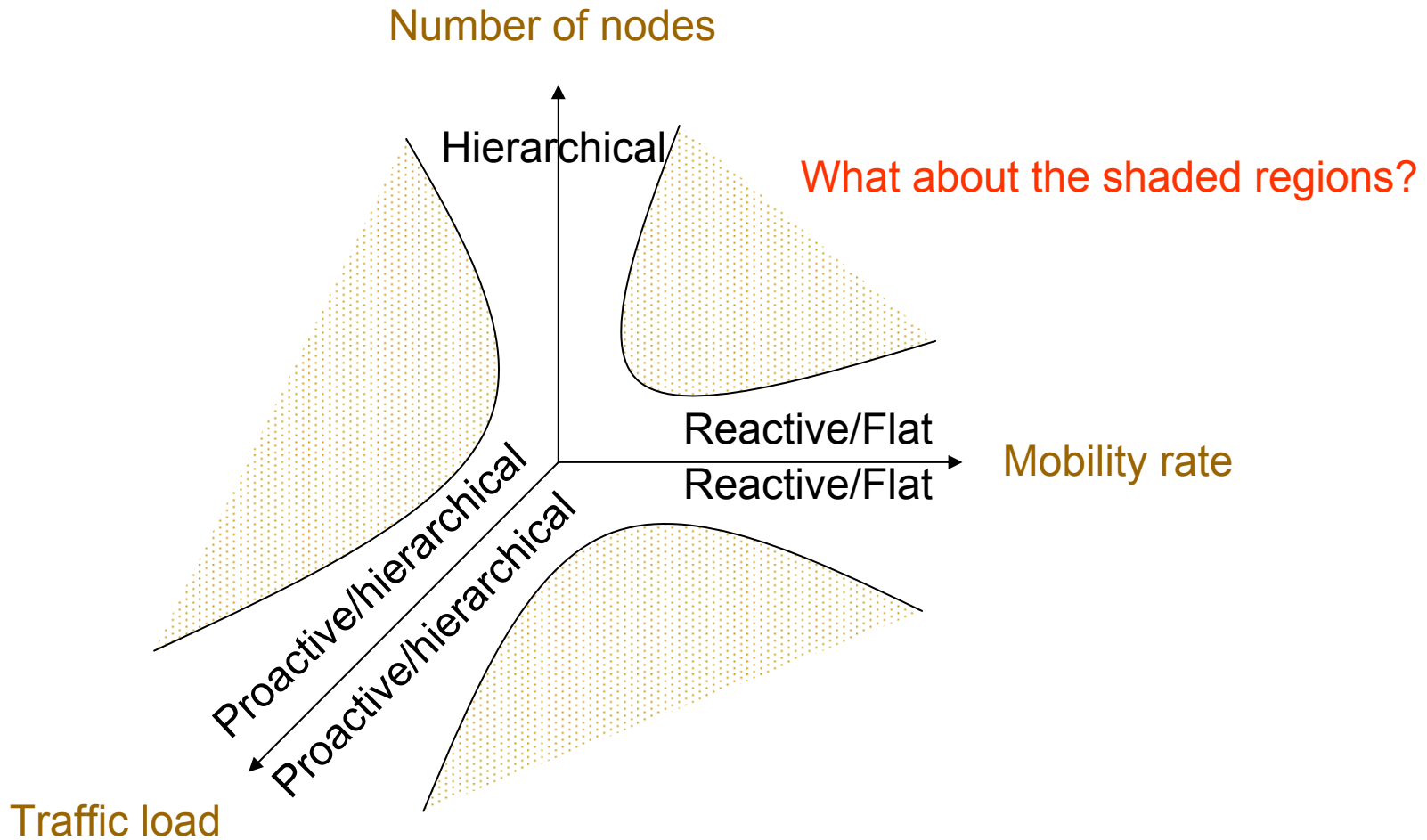
# Trade-offs

- Complexity
  - Hierarchical structures are more complex than that of flat
- Overhead
  - Hierarchical structures produce significant configuration overhead at the expense of efficient communication overhead; while
  - Flat structures produce no configuration overhead at the expense of significant communication overhead
- Scalability
  - Hierarchical structure are more scalable than that of flat as the number of nodes increases
- What about storage requirement? Fairness?

# Other Issues

- Route caching
- Source routing vs. hop by hop routing
- Local route repair
- Periodical Beacons and battery life
- Unidirectional link
- Shortest path is not enough!
  - Power-aware routing
  - Stability-based routing
- Load balancing and traffic shaping
- Effect of mobility model and traffic pattern on protocol performance

# Protocol scalability

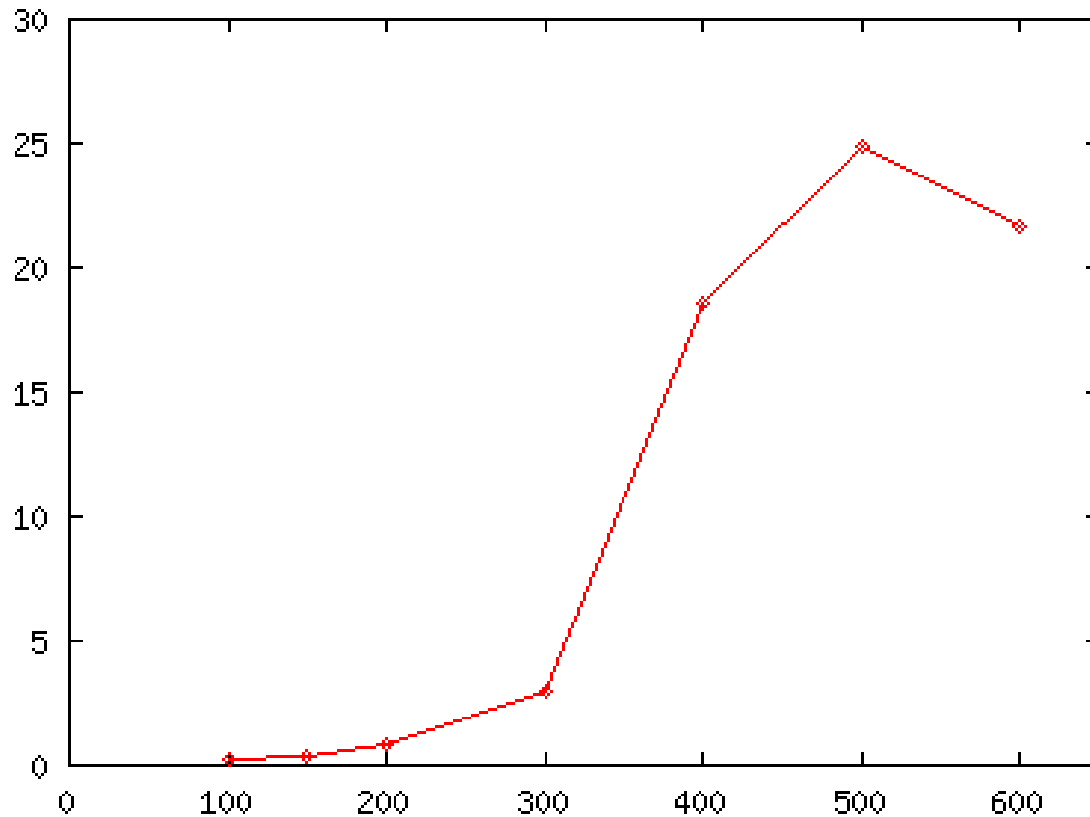


# Motivation of Position-based Routing

- Determining relative/absolute positions of nodes in indoor/outdoor becomes practical
  - **Relative:** distance estimation on the basis of incoming signal strength or time delay in direct communication [[bulusu00](#),[capkun01](#)]
  - **Absolute:** using global positioning system (GPS) through a satellite communication
  - Such position information can either be:
    - Physical ( $47^{\circ}39'17''$  N by  $122^{\circ}18'23''$  W)
    - Symbolic (in the kitchen, next to a mailbox)
- Lack of scalability
  - Communication overhead for route generation due to node mobility is quadratic as the network size increases[[stoj02](#)]

# Motivation: Flooding Overhead

Avg. packets transmitted  
per node per second



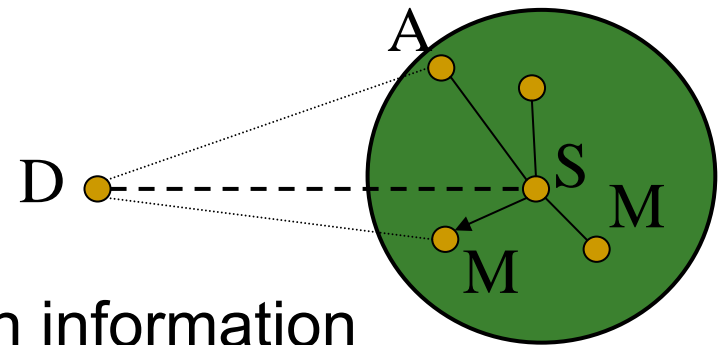
Ref. GLS[Li]

Number of nodes



# Motivation

- Large network with high mobility and traffic load
  - Localized algorithm (distributed in nature)
    - Local behavior achieves global objectives [[stojm02](#)]
    - Think globally, act locally [[streenstrup02](#)]



- Require accurate local location information
- Approximation of the position of destination
- The source (S) forwards a data packet to at least one neighbor (A or M or both) closest to the destination (D)

# Position-based Routing [[finn](#),[mauve01](#),[stoje02](#)]

- Requires location-sensing techniques [[hightower01](#)]
  - **Triangulation:**
    - Lateration measures multiple distances between known points
    - Angulation measures angle to points with known separation
  - **Proximity:** measures nearness to known set of points
  - **Scene analysis:** examines a view from a particular point
- Incorporates three fundamental building blocks:
  - **Location service:** determines the position of destination
  - **Forwarding strategy:** determines the next hop
  - **Recovery procedure:** determine the next hop in case of failure
  - The first two blocks can either be performed jointly (DREAM, LAR) or separately

# Location Service

- A process that enables the network to *track* and *locate* the current **position** of a node
- Operating on **location server**/directory/database
- Location service is a combination of:
  - **Location update**
    - in charge of tracking
    - occurs when a node changes location
  - **Location search (location request/reply)**
    - in charge of locating
    - occurs when a host wants to communicate with a mobile node whose location is unknown to the requesting node
- What are the different design choices of location service?

# Location Service Design Choice

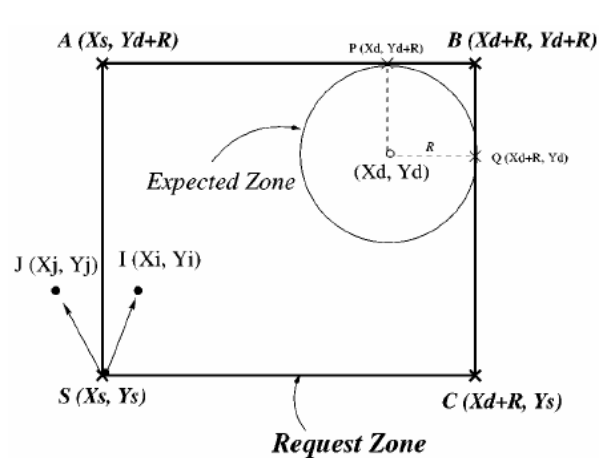
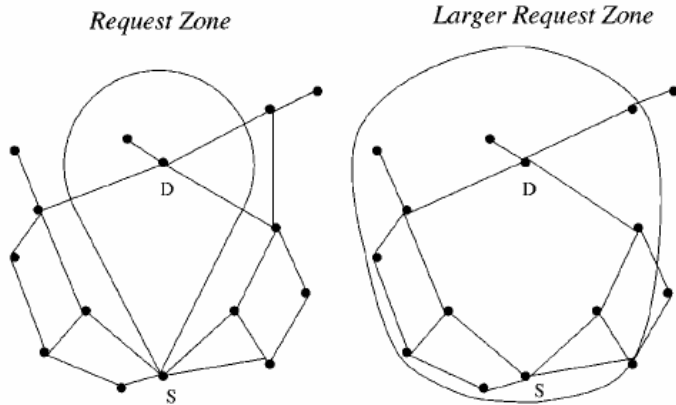
- Do I keep *track* of positions to all destinations, or instead *locating* only those of immediate interests?
  - **Proactive**: full location update and no location search, DREAM
  - **Reactive**: no location update and full location search, LAR
  - **Hybrid**: moderate location update and location search
    - How many nodes host the service?
    - How many positions are maintained by the location server?
- Trade-offs exist between the delay performance of location search and communication overhead of location update

# Location-aided routing (LAR)

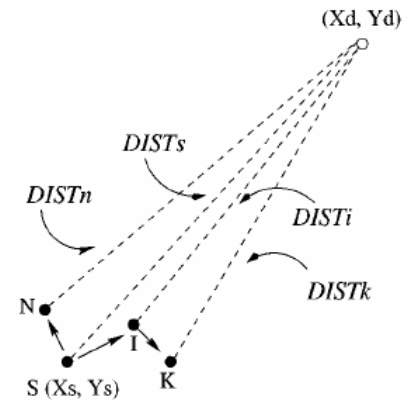
- Idea: using **location information** to limited flooding
  - Node S knows that
    - Node D was at location L at time  $t_0$
    - Traveling with average speed  $v$
    - The current time is  $t_1$
  - Determine the expected zone
    - By a circle centered at  $L_D(t_0)$  with radius  $v \times (t_1 - t_0)$
    - Refine the expected zone if some trajectory information is available (D is traveling towards north)
  - Determine the request zone for route request
    - Greater or equal than the expected zone
    - Other regions around the expected zone
    - Note: request zone affects the probability of successful route request

# Location-aided routing

- No guarantee that a path can be found consisting only of the hosts in a chosen request zone
  - timeout
  - expanded request zone
- Trade-off between latency of route determination and the message overhead



LAR Scheme 1



LAR Scheme 2

# A distance routing effect algorithm for mobility

- Proactively disseminate location information
  - Each node maintains a location table of all nodes
  - Flood if no entry for destination in table, otherwise
  - Forward to the neighbors in the direction of the destination
  - If no one-hop neighbor is found in the required direction, run the recovery procedure (not specified in DREAM!)
- Direction is the line between S and D with the angle  $\varphi$ 
  - The angle  $\varphi$  is determined by an expected region
  - Expected region centered at  $L_D(t_0)$  with radius  $r = v_{max} \times (t_1 - t_0)$

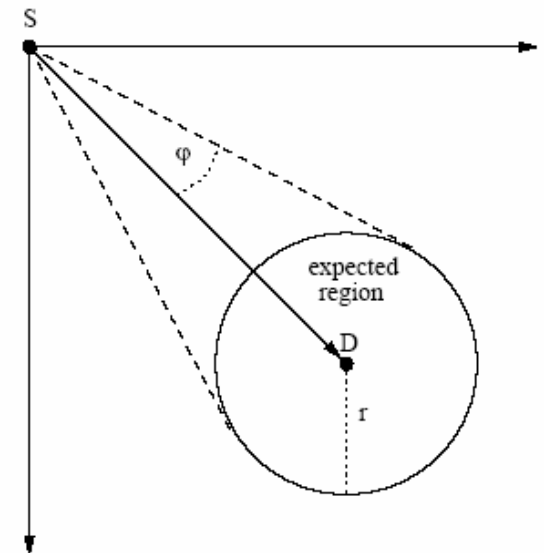
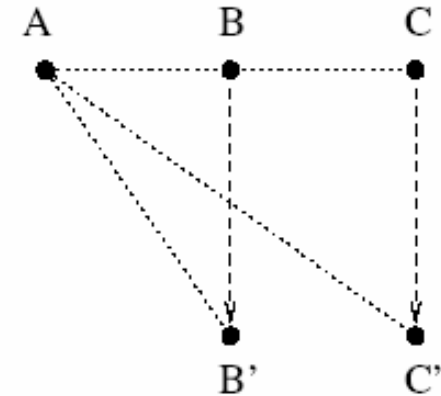
# DREAM

## ■ Distance Effect

- The farther away a nodes gets, the slower it appears to move
- Update more frequently the closed by nodes (packet age)

## ■ Mobility Effect

- The faster a node moves, the higher is the update rate
- Adjust the frequency of update as a function of mobility rate
- No bandwidth wastage for no movement

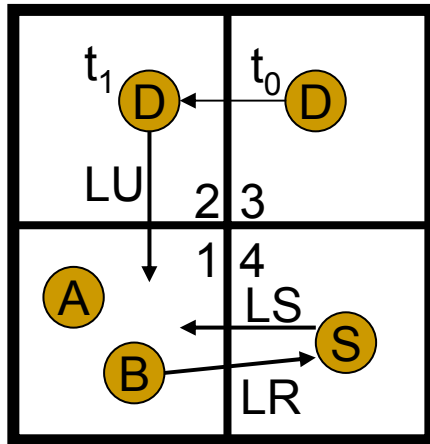




# Hybrid Location Server

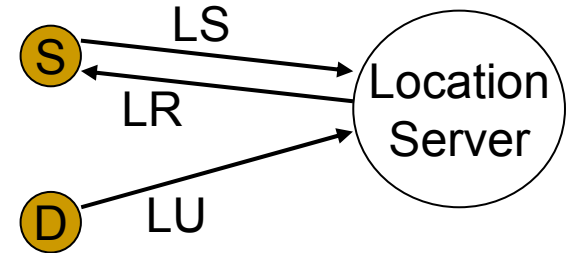
- **Single home zone:** e.g. Mobile IP, virtual home region
  - Define as a set of nodes, in a rectangular or a circle with radius  $R$ , close to a known position
  - This position is determined based on a well-known hash function
  - All for some if home zones are uniformly distributed
- **Quorum system:** e.g. uniform QS, double circle,
  - Replicates location information at multiple nodes that are acting as location servers
  - Location updates (write operation) are sent to a subset of nodes (quorum)
  - Location search (read operation) requests potentially a different subset
  - Such subsets are designed such that their intersection is non-empty
  - Can be configured to be all-for-all, all-for-some, or some-for-some
- **Multi home zone:** e.g. grid based, graph-based
  - Replicates location information at multiple positions in the area of ad hoc networks

# Hybrid Location Server

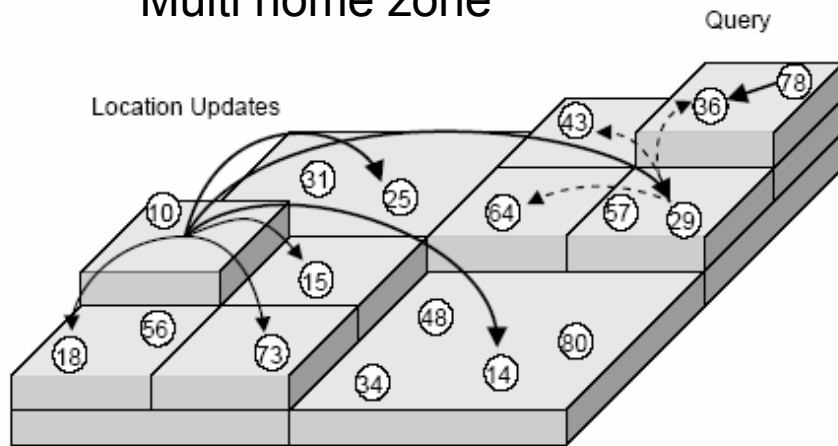


Multi home zone

1. LS(D) = zone 1
2. D(t<sub>0</sub>) @ zone 3
3. D(t<sub>1</sub>) @ zone 2
4. LU(D) @ LS(D)
5. LS(S) @ LS(D)
6. B sends LR(D) to S

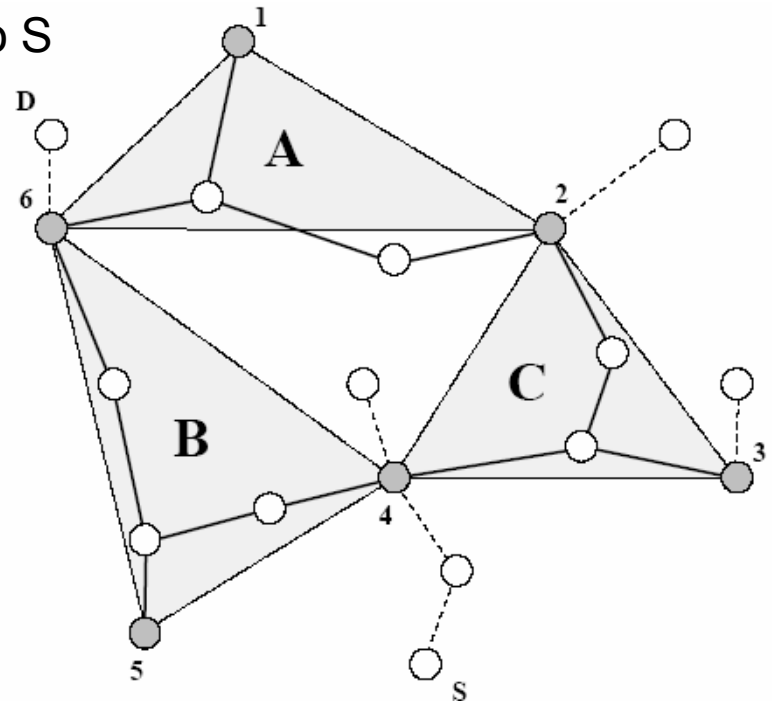


Single home zone



GRID: Multi home zone

Least ID greater than a node's own ID



Quorum System

# Complexity metrics [mauve03]

- **Type** indicates how many nodes host the location information and for how many nodes they maintain location information
- **Communication complexity** describes the average number of hops required to update or search a node's location
- **Time complexity** measures the average time it takes to perform a location update or search
- **State volume** represents the amount of state required in each node to maintain the location information represents state volume
- **Localized information** means that a higher density or a better quality of the location information is maintained near the position of the node
- **Robustness** indicates the failure of how many nodes can render the location of a given node inaccessible
- **Implementation complexity** describes how well the location service is understood and how complex it is to implement and test it

# Complexity comparison [mauve03]

Criterion	DREAM	Quorum System	GLS	Homezone
Type	All-for-All	Some-for-Some	All-for-Some	All-for-Some
Communication Complexity (Update)	$O(n)$	$O(\sqrt{n})$	$O(\sqrt{n})$	$O(\sqrt{n})$
Communication Complexity (Lookup)	$O(c)$	$O(\sqrt{n})$	$O(\sqrt{n})$	$O(\sqrt{n})$
Time Complexity (Update)	$O(\sqrt{n})$	$O(\sqrt{n})$	$O(\sqrt{n})$	$O(\sqrt{n})$
Time Complexity (Lookup)	$O(c)$	$O(\sqrt{n})$	$O(\sqrt{n})$	$O(\sqrt{n})$
State Volume	$O(n)$	$O(c)$	$O(\log(n))$	$O(c)$
Localized Information	Yes	No	Yes	No
Robustness	High	Medium	Medium	Medium
Implementation Complexity	Low	High	Medium	Low
Abbreviations: n=Number of Nodes c=Constant				

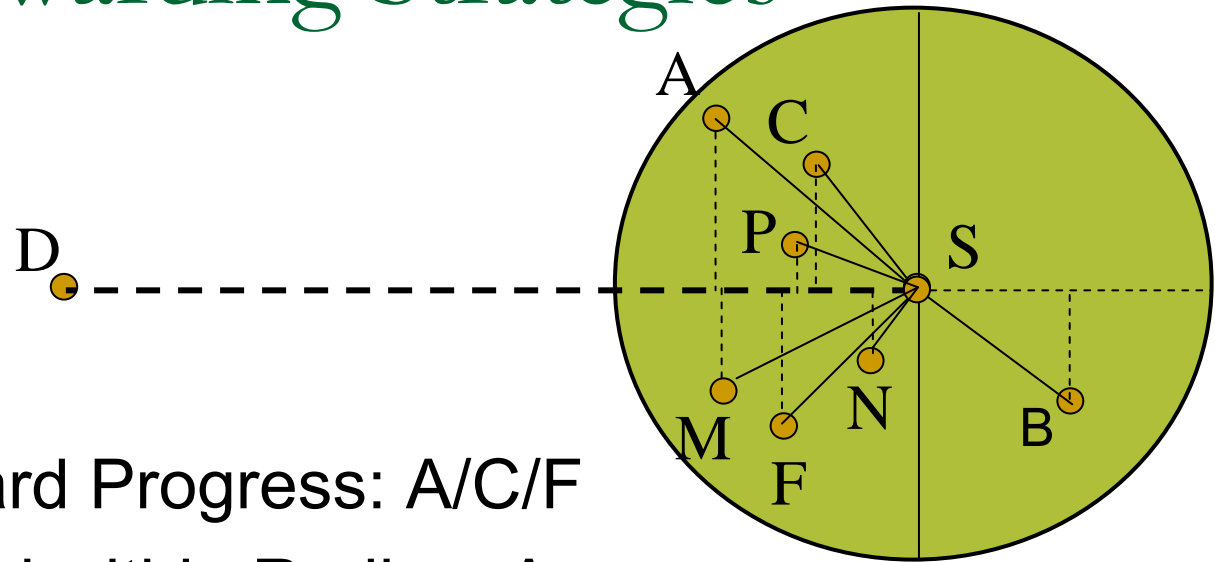
# Location Update/Search Schemes

- Temporal resolution: frequency at which a location update/search is sent
  - Timer-based: periodic, threshold
  - (predictive) Distance-based: (velocity) location, threshold
  - Profile, movement, state (a combination)
- Spatial resolution: where/how far a location update/search should travel before it is discarded
  - Blanket polling
  - Shortest distance first
  - Sequential (group) paging
- [[aky99](#), [tabbane97](#), [wong00](#), [zhang04](#)]
- Note: route discovery can be used for location search

# Forwarding Strategy

- To which node(s) should I forward packet P?
  - **Greedy forwarding:** forwards P to exactly one neighbor closer to the destination than the forwarding node itself, e.g. MFP, NFP
  - **Restricted directional flooding:** forwards P to more than one neighbor, e.g. DREAM, LAR
  - **Hierarchical forwarding:** forwards P through a set of known positions (e.g. anchor, location proxies) that lead to the final destination, e.g. Terminodes, Grid
    - Apply topology-based routing (mainly proactive) for short distance and position-based (mainly greedy) for long

# Greedy Forwarding Strategies



- Random Forward Progress: A/C/F
- Most Forwarded within Radius: A
- Nearest Forward Progress: N
- Geographic distance: M
- Nearest Closer: N
- Compass (directional) routing: P
- Are all of these approaches loop-free?

# Terminodes [blazovic00]

- Combines topology- and position-based routing
- Routing is done at two levels:
  - For short distance routing (# of hops): route the packets according to a proactive distance vector algorithm
  - For long term distance routing, a greedy forwarding is used
  - Note: once the packet gets close to its final destination, it switches to the short distance routing
- To prevent local maximum, the sender includes a list of anchor nodes into the header through which the packet should visit during forwarding
  - Packet forwarding is greedy between two anchor nodes
  - Could also be named as position-based source routing
  - Note: the sender should know the sequence of anchor nodes that lead to the final destination



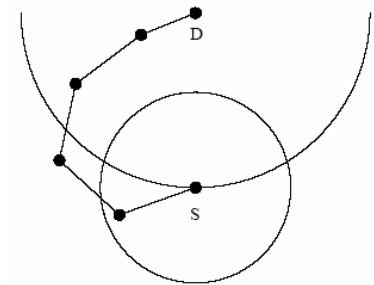
# Complexity comparison

Criterion	Greedy	DREAM	LAR	Terminodes	Grid
Type	Greedy	Restricted Directional Flooding	Restricted Directional Flooding	Hierarchical	Hierarchical
Communication Complexity	$O(\sqrt{n})$	$O(n)$	$O(n)$	$O(\sqrt{n})$	$O(\sqrt{n})$
Tolerable Position Inaccuracy	Transmission Range	Expected Region	Expected Region	Short-Distance Routing Range	Short-Distance Routing Range
Requires All-for-All Location Service	No	Yes	No	No	No
Robustness	Medium	High	High	Medium	Medium
Implementation Complexity	Medium	Low	Low	High	High

- **Tolerable position inaccuracy:** degree of inaccuracy w.r.t. the position if the receiver
- **Robustness:** if the failure of a single intermediate node does not prevent the packet from reaching its destination

# Recovery procedures

- Deals with the situation where forwarding strategies may fail if there is no one-hop neighbor closer to the destination than the forwarding node itself (occurs in sparse networks)
  - Packet reaches a local maximum
  - Local route discovery
  - Closest neighbor in backward (least negative BW)
  - Planner sub-graph, e.g. Gabriel graph
    - There is an edge between two nodes  $u, v$  iff the disk( $u, v$ ) including boundary contains no other points
  - Reinitiate from source with a random selection of the forwarding node



# Other issues

- How to avoid empty location server
- How to adjust the size of location server
- What happens if no location reply is received?
- Who determines the next hop?
  - Sender or receiver
- Location privacy?

# Routing and topology control Issues

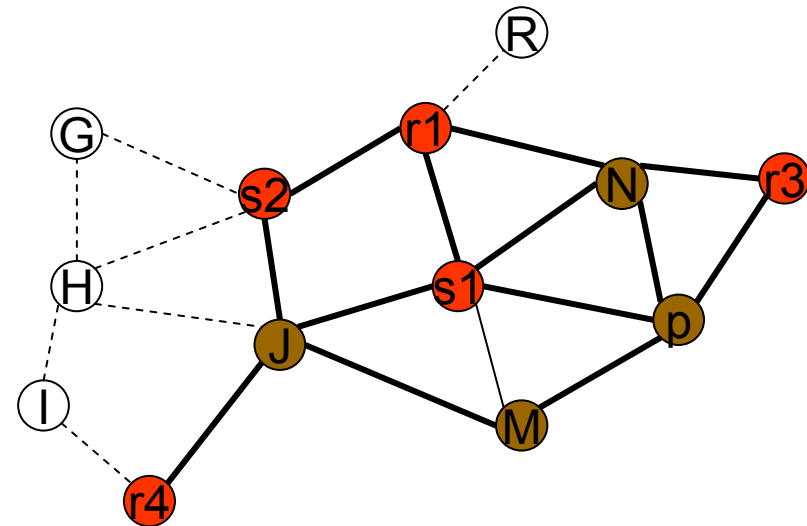
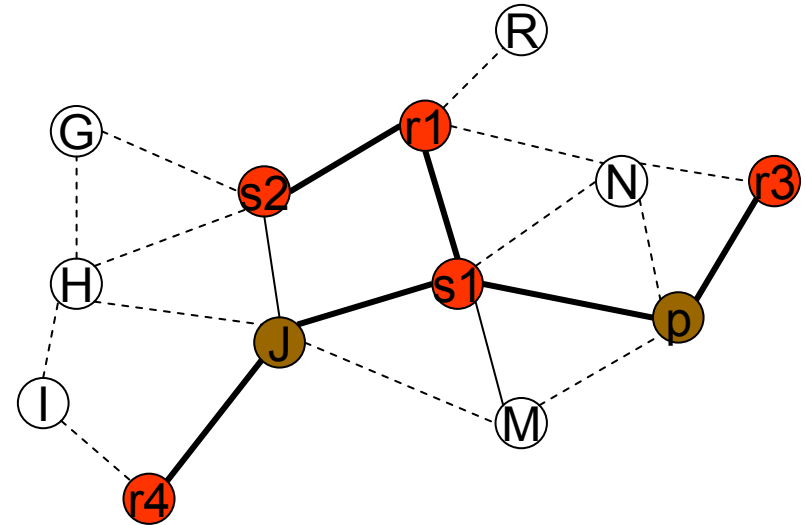
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# Multicasting [li04]

- Potential applications in MANET require one-to-one, one-to-many, and many-to many communication models.
- One-to-many and many-to-many require efficient multicasting to support group-oriented computing
  - Community centric: multi-player on-line gaming
- There exists three ways to transmit packet  $P$  to multiple receivers:
  - **Unicasting**: sends a separate copy of  $P$  to each receiver
  - **Broadcasting**: floods a copy of  $P$  throughout the network
  - **Multicasting**: transmits  $P$  to a group of hosts identified by a single destination address [cordeiro 03]
- Which approach is the best?

# Multicast Issues [wu]

- Operation
  - Group-demand
  - Traffic-demand
- Group membership management (dynamic join/leave)
  - Tree-structure
    - Source-based (figure above ↗)
    - group-shared
  - Mesh-structure (figure below ↘)
    - Multiple path between any source and receiver pair
  - State-less
    - Explicitly mention the list of receivers
- Forwarding strategy
  - On tree
  - Unicasting
  - Boadcasting



# Geocasting [jiang02, maihofer04]

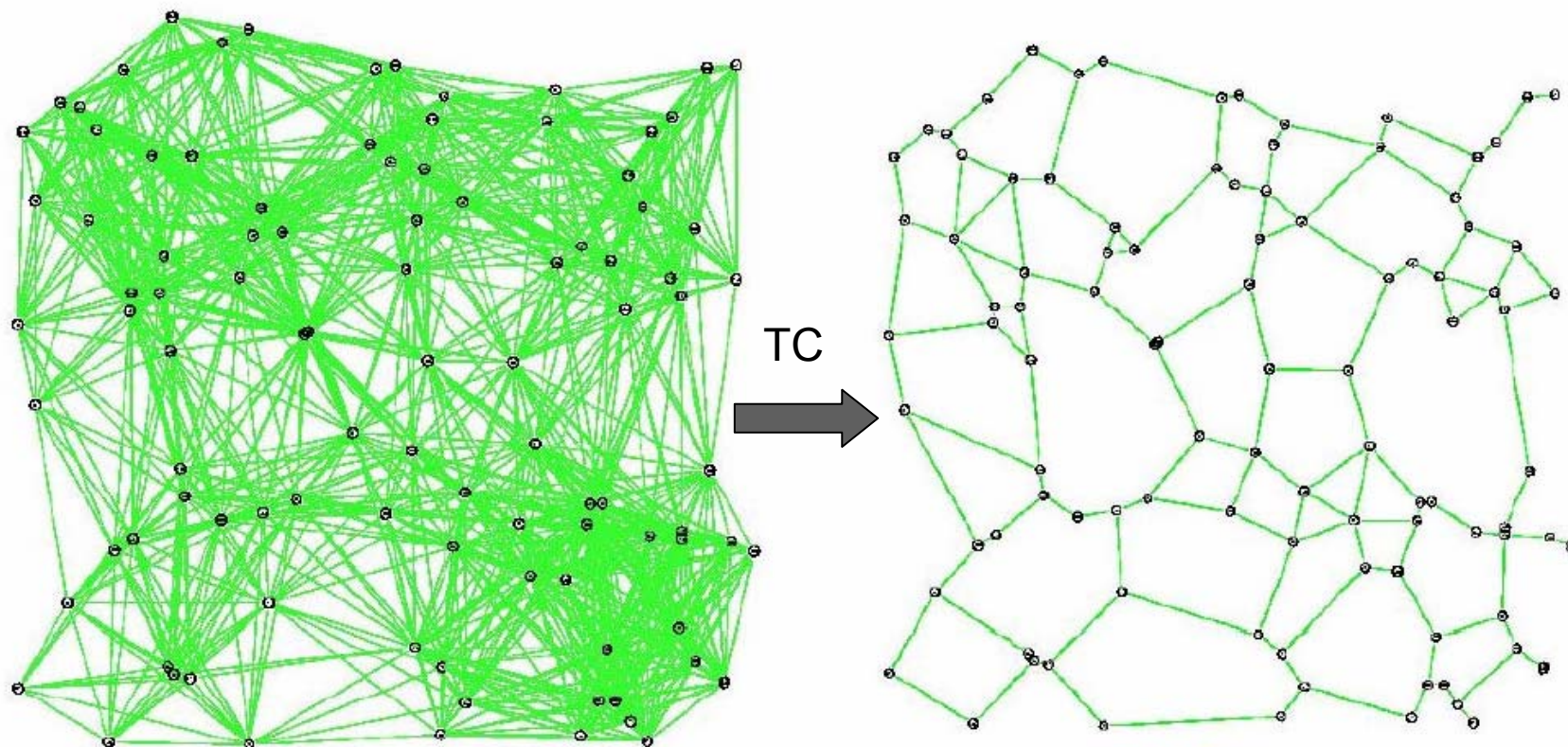
- Deliver packet  $P$  to a group of nodes located within a specific geographical location: called **geocast region**
  - Public safety applications, Fire, accident
    - Geocast emergency information within a given radius
  - Finding nearby friends, or geographical advertising
- A variant of multicasting problem
- Group membership is implicitly defined as the set of nodes within a geocast region at a given time
- Protocols differ in how they transmit information from a source to the geocast region:
  - Broadcasting or Unicasting
- Could multicasting be used instead of geocasting?
- How to distinguish between different groups within a geocast region?

# Topology Control

- Inappropriate topology can significantly reduce the network capacity and performance
  - Too dense network limits spatial reuse factor, and drains battery life
  - Too sparse network risks of partitioning
- To adjust the **network topology** as nodes move and environment changes subject to certain **constraints**
- Network topology,  $G(V, E)$ 
  - **Link**: range assignment problem → power control
  - **Node**: dominating set problem → clustering scheme
  - Both approaches make the graph  $G$  sparser, same objective
- Constraints:
  - **Link**: power consumption, and network capacity
  - **Node**: load reduction, and load balancing



# Topology Control



# Power Control [santi04]

- Whether all nodes have the same radii?
  - **Homogeneous:**
    - Given  $n$ , what is the minimum value of the transmitting range that ensures connectivity? or
    - Given a transmitter technology, how many nodes must be distributed in order to obtain a connected network?
    - Min connectivity range is called **critical transmission range**
  - **Non-homogeneous:**
    - Given  $n$ , determine a **connecting** (potentially asymmetric) range assignment set with **minimum energy cost** ?
    - Given a graph  $G$ , determine a so called **routing subgraph**  $G'$  of  $G$  such that the power of the path connecting any two vertices is minimized

# Homogenous Power Control

- Whether nodes' position are known?
  - Position-based:
    - CTR is the longest edge of the Euclidean MST
  - Non-position-based:
    - Probabilistic approaches
      - Given  $n$ , determine the transmission range such that the network is connected with a high probability
      - Applied probability theories are used as a tool:
        - Continuum percolation
        - Occupancy theory
        - Geometric random graph

# Non-Homogenous Power Control

- Main properties of subgraph  $G'$ :

- Connected
- Energy efficient
- Localized
- Low stretch factor

$$\text{Max} \frac{C_G(u, v)}{C_{G'}(u, v)}, \forall u \neq v \in V$$

- Measure of the increase in cost function,  $C$ , due to communicating through  $G'$  instead of  $G$
- Cost function can be energy, hop, distance
- [rajaraman]

# Non-Homogenous Power Control

- **Spanner** subgraphs best describes the problem of designing topology with low stretch factor
  - A spanner is a subgraph  $G'$  of  $G$  such that the distance between any two nodes is within a constant factor, i.e.  $O(1)$ , of the distance between two nodes in  $G$
  - Topology with a  $O(1)$  distance stretch factor has a  $O(1)$  energy stretch factor
    - The power attenuates as distance raised to an exponent ( $\alpha$ )
  - Examples of routing proximity subgraphs:
    - Relative Neighbor Graph (RNG)
    - Gabriel Graph
    - Yao Graph
    - (Restricted) Delaunay triangulation

# Proximity Graphs

## ■ RNG Graph

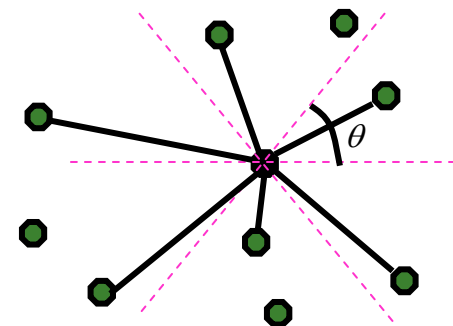
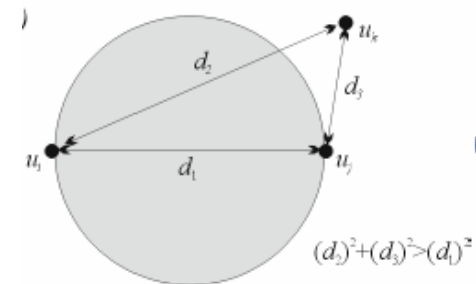
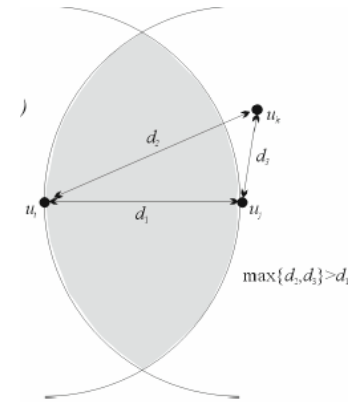
- An edge between  $u$  and  $v$  exists if for any node  $w$   
 $\max \{ d(u,w), d(v,w) \} > d(u,v)$

## ■ Gabriel Graph

- An edge between  $u$  and  $v$  exists if for any node  $w$   
 $d^2(u,w) + d^2(v,w) > d^2(u,v)$

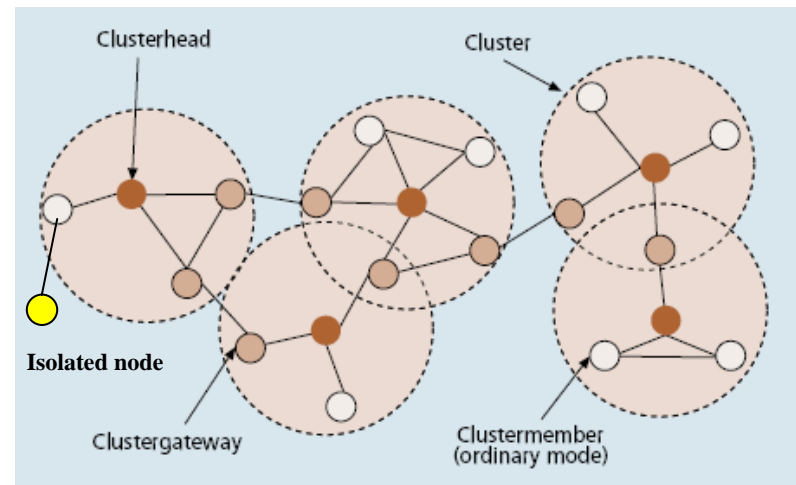
## ■ Yao Graph

- Partition the space into sectors of a fixed angle  $\varphi$
- Connect the node to the nearest neighbor in the sector



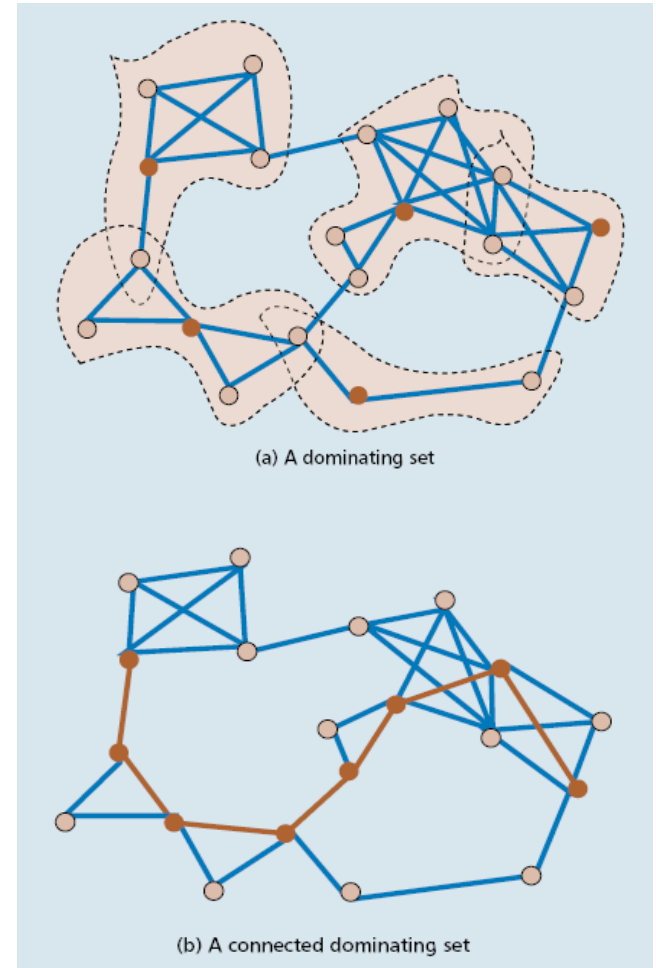
# Clustering Scheme [yu05]

- A hierarchical structure is essential for protocol scalability and for performance guarantee
  - Facilitate spatial reuse: improve network capacity
  - Virtual backbone: reduce overhead, improve stability
- Partitioning network into a set of logical / physical groups or zones
- Role assignment:
  - Clusterhead
  - Clustergateway (relay)
  - Clustermember
  - Isolated node



# Clustering Scheme

- In graph theory, the **Dominating Set** problem best describes the clustering scheme
- Determining a subset of nodes such that each node is either a DS or adjacent to DS node
  - $G=(V,E), DS(G)=G'(V', E')$
  - $\{ V' \in V, \forall u \in V-V', \exists v \in V' \mid (u,v) \in E \}$
- Connected Dominating Set
- Minimum CDS
- M(C)DS is **NP-Complete**
  - Heuristics approach





# Sub-optimal Clustering Schemes

- Find a (C)DS that is “close” to minimum
  - Sub-optimal DS → optimal CDS iterative
  - Sub-optimal CDS → optimal CDS purging
  - Sub-optimal DS → optimal WCDS
  - Sub-optimal MIS → optimal CDS
- Weakly connected dominating set (WCDS)
  - Relax the requirement of direct connection between neighboring dominating set
- Maximum independent set (MIS)
  - No two vertex in the dominating set are adjacent

# Clustering Scheme Issues

- Time and communication complexities of clustering: formation and maintenance
- Stability to nodal mobility and traffic load
- Clusterhead existence
- Clusterhead election criteria:
  - Any nodal information: ID, Deg, # of local DS, Mobility, Energy, Load, security-related metric
- One-hop or multihop

# Nodal State Information

- ID
  - Degree
    - Logical or physical?
  - State
    - Load (buffer state)
    - Power level (transmission radii)
  - Velocity
  - Absolute or relative position
  - Trajectory
- 
- Local information
    - Average state of neighboring nodes
    - SNR, signal stability
  - Global information
    - Average state of the network